

# String Cosmology: A Review

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We give an overview of the status of string cosmology. We explain the motivation for the subject, outline the main problems, and assess some of the proposed solutions. Our focus is on those aspects of cosmology that benefit from the structure of an ultraviolet-complete theory.

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# 1 Yet Another String Cosmology Review

The past decade has seen tremendous advances in cosmology. The discovery of dark energy [1] crushed widely-held expectations that some unknown mechanism might set the cosmological constant to zero. At the same time, a flood of data on the cosmic microwave background (CMB) [2] has revealed an early universe in striking agreement with the basic predictions of inflationary scenarios. The resulting paradigm of a universe undergoing inflation [3] at early times, and dominated by cold dark matter and dark energy at late times, has sometimes been referred to as a Standard Model for cosmology.

However, the situation is far more mysterious than the comparison with the Standard Model of particle physics would suggest. Inflation provides a robust field-theoretic mechanism that addresses many cosmological problems – and that made predictions [4] strikingly verified by CMB experiments – but the data does not yet pin down anything close to a precise model. Similarly, we lack a complete understanding of dark energy; the best explanation to date of the dark energy scale is a selection effect [5]. Both of these subjects, although modeled at a basic level within the framework of effective field theory, are closely connected to challenging issues in quantum gravity.

At the same time, substantial theoretical progress in string theory has brought forth a diverse new generation of cosmological models, some of which are subject to direct observational tests. One key advance is the emergence of methods of moduli stabilization. Compactification of string theory from a total dimension  $D$  down to four dimensions introduces many gravitationally-coupled scalar fields – moduli – from the point of view of the four-dimensional theory. Runaway or light moduli are extremely problematic in cosmology, and in any realistic model they must be metastabilized by an appropriate balance of forces. Extensive work in the subject of moduli stabilization (see e.g. [6, 7, 8, 9, 10, 11, 12], as well as the reviews [13, 14, 15, 16, 17, 18, 19] and references therein) has shown that in many classes of compactifications, the four-dimensional effective action contains a rich set of potential energy terms that plausibly contribute the requisite forces [9, 10, 11, 12]. This realizes the possibility of a “discretuum” of vacua introduced in [20] (see also [21]).

Some earlier developments in string cosmology relied on the hope that whatever mechanism eventually stabilized the moduli would not have side effects for models of inflation and dark energy. We know now that this hope, though not unreasonable, is violated in a wide class of models: the details of moduli stabilization do have important effects in cosmological models. Nevertheless, moduli stabilization can now be studied in semi-explicit constructions, and this gives current models a certain degree of completeness and realism.

This confluence of observational and theoretical advances makes the present situation rather exciting. Even if there are no further surprises, observational advances will certainly zero in on a tiny fraction of the present parameter space; moreover, the techniques exist to

make relatively robust models of the resulting phenomena in string theory.

In this review we will not attempt to give a comprehensive assessment of the status of inflation, let alone of more general cosmological model-building. Indeed, the recent period has seen a number of useful reviews of the subject, which complement ours in some ways [22]; this leaves us the freedom to comment most extensively on the aspects of string cosmology with which we are most familiar. It bears mentioning that, although inflation is by far the most compelling explanation for the observed properties of the very early universe, its status is the subject of some debate, and most authors find that some degree of fine-tuning appears to be necessary. Thus, it is worth keeping in mind the possibility of an entirely different solution to the Big Bang problems.

More generally, there are important questions in string cosmology that inflation renders essentially inaccessible experimentally, such as the resolution of spacelike singularities, or phase transitions connecting different limits of string theory. Microscopic physics is clearly relevant to these questions, which are motivated by intellectual interest regardless of near-term testability.<sup>1</sup> Moreover, the possibility remains open that their resolution could introduce consistency conditions or other effects relevant also at later times, perhaps as initial conditions for inflation. We will therefore include a discussion of these issues in §2, and then move on to a survey of some attempts at realistic model-building within string theory. Before moving to these developments, however, let us flesh out the basic reasons for the mutual relevance of string theory and cosmology.

## 1.1 String theory and cosmology

Inflation provides a solution to the flatness and horizon problems within the framework of quantum field theory (QFT) and general relativity (GR). Moreover, in so doing it screens from observational view much of the physics of the ultraviolet (UV) completion of this framework, whatever that might be. Indeed, inflation explains the *absence* of observable relics, such as monopoles from possible extensions of the Standard Model. One may wonder, therefore, whether string theory, as a candidate UV completion of particle physics and gravity, should play much of a role in cosmology at all. However, there are several reasons for greater optimism, to which we now turn.

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<sup>1</sup>Perhaps it is worth emphasizing in this regard that at the time that inflation was proposed, there was little or no confidence in the possibility of measuring its consequences; one can hope that similar surprises in observational accessibility will arise in the future.

### 1.1.1 *Utility of string theory in theoretical cosmology*

There are several theoretical motivations to incorporate string theory into cosmological model building. First, the observed expansion of the universe, extrapolated backward in time using the equations of GR and QFT, inevitably hits a regime where these descriptions break down [23]. The corresponding spacelike singularity requires physics beyond the Standard Model and GR to resolve. For this reason, and also because of the causal structure of spacetimes with inflation and dark energy, we lack a coherent framework for analyzing cosmology from start to finish. Second, there is the possibility that the degrees of freedom appropriate to describe cosmological spacetime could be understood at a more fundamental level by enumerating microscopic degrees of freedom that account for the Gibbons-Hawking entropy, in the same way that black holes have been illuminated by the determination of the microscopic origin of the Bekenstein-Hawking entropy [24] in certain cases. Finally, at a more practical level, many field-theoretic cosmological models involve ranges of energy scales and scalar field strengths which reach large enough values that generic string or Planck-scale corrections become significant.

### 1.1.2 *Cosmology as a test of string theory*

Conversely, cosmology is a natural place to seek concrete tests of string models. First of all, purely in comparison to collider experiments, cosmological observations hold greater promise for testing string theory. A natural energy scale for inflation is around the GUT scale, and an observation of primordial tensor fluctuations in the CMB would establish beyond doubt that the CMB fluctuations were generated at such energies. No planned terrestrial experiment can reach a fraction of this energy. Hence, the decoupling of high-energy phenomena strongly suggests that unless by some strange chance the string scale is extremely low, signals of string theory will be seen, if they are seen at all, in the sky.

This must not be taken to mean that CMB experiment is either a direct or a guaranteed probe of string theory. Almost any signal that can arise in a string model can arise in a suitable low-energy effective quantum field theory. Distinguishing these possibilities is highly nontrivial and could be impossible in many cases. With this in mind, there are still two avenues for a possible test. In fortunate circumstances, some phenomenon does not fully decouple at low energies; cosmic strings, which are topological defects, are an important example. Another way to use cosmological observations to constrain string theory is to check for signals which are natural or generic in string-derived effective Lagrangians, but highly unnatural from a conventional field-theory viewpoint. Observation of such a signal would be suggestive, at the very least. A specific form of this strategy is to find signals that *cannot* arise in effective field theories derived from certain string theory constructions. As an example, in many – but *not* necessarily all – string inflation models, the primordial tensor

signal is very small, as we review in §3.2.3. Hence, an observation of primordial tensors would eliminate the great majority of presently-known string inflation models. Eliminating classes of string constructions in this way does not amount to a test of string theory itself, but would nevertheless play a valuable role by restricting the currently formidable range of possibilities of the theory.

In this spirit, the fact that inflation models require control over the action at a level sensitive to Planck-scale corrections (as in the supergravity eta problem reviewed in §3.2.2) may provide information about such microphysical effects, at least in specific frameworks for model building. Of course, with only a small number of operators constrained in this way, the problem of tying observations to string theory is still enormously underdetermined.

## 2 The Initial Singularity in String Theory

A UV completion of GR is most directly relevant at very early times, and becomes crucial at the initial singularity. Our understanding of the resolution of spacelike singularities is very limited, but recent work has shown how the new degrees of freedom introduced by string theory play a significant role, plausibly resolving the singularity in special examples. Without embarking on a comprehensive review of this large subject (see [25, 26, 27, 28] for some recent lectures and reviews), let us here mention some concrete ways in which string-theoretic microphysics intervenes on the way back to the would-be initial singularity.

### 2.1 Approaching the singularity in the effective theory

The low energy field content of string theory affects the approach to a spacelike singularity as explained in e.g. [29]. The inclusion of  $p$ -form fields as well as curvature leads to chaotic dynamics in this regime, generalizing the BKL analysis of the approach to the singularity in four-dimensional general relativity [30] (see e.g. [31] for recent numerical studies). The fields bounce around in a potential consisting of a sum of exponential walls determined by the fluxes and curvature terms, leading to a billiards problem; this is related to the fact that upon dimensional reduction of a gravity theory, the potential energy is exponential in the canonically normalized scalar fields descending from the metric and other modes. In a realistic setting, the number of times the field bounces off a wall is limited, but conceptually the effect is quite interesting and suggests the possibility of an enhanced symmetry near the singularity.

Another important feature of many cosmological models is a regime of eternal inflation at very early times. A version of this process that is controlled within effective field theory arises in the presence of metastable vacua, which are a feature of string-theoretic models fixing moduli to obtain (metastable) de Sitter space [11, 12], described further in §6 below.

Attempts to describe eternal inflation holographically, or to determine a probability measure in this context, include [32, 33, 34]. Two of the main issues are as follows. First, heuristically one might expect the most rapidly-inflating region to give the dominant probability, because of its exponentially larger volume. However, this description is not automatically gauge invariant in general relativity, and in addition there are limits to predictivity in any closed quantum mechanical system. Second, in the regime described well by effective field theory and GR, the causal structure of an eternally inflating spacetime is such that no single observer can access the full geometry. Operationally, then, it might make the most sense to consider a formulation based on the causal patch of a single observer. Various proposals addressing these issues have been put forward, and the subject is an active area of current research. Once a mathematically well-defined framework is obtained, one would like to know if it is uniquely specified, what predictions it makes, and whether or not the results are sensitive to initial conditions.

## 2.2 Perturbative string theory and winding states

Eventually, a treatment based on QFT and GR breaks down, either when the Hubble expansion rate increases to the scale of some new physics, or when features in the spatial three-manifold shrink to the string scale (in a background with weak string coupling  $g_s \ll 1$ ) or the Planck scale (in a background with  $g_s \sim 1$ ). In particular, perturbative string degrees of freedom become important in large classes of examples. Consider the spacetime

$$ds^2 = -dt^2 + a^2(t)ds_{\mathcal{M}_3}^2 + ds_{\perp}^2 \quad (2.1)$$

where  $\mathcal{M}$  is some three-manifold. Almost all compact spatial manifolds  $\mathcal{M}_3$  – in fact<sup>2</sup> all but the three-sphere  $S^3$  – include topologically nontrivial one-cycles, which support new single-string states corresponding to strings wound around these cycles. Indeed, there is a well-defined mathematical sense in which most compact manifolds are hyperbolic [35] and hence have a fundamental group of exponential growth [36].<sup>3</sup> That is, the number of closed geodesics as a function of their length  $l$  grows exponentially with  $l$ :

$$\rho(l) \sim e^{l/l_0} \quad (2.2)$$

where  $l_0$  is of order the curvature radius, and we neglect power-law prefactors. Thus, since winding string masses scale like  $l/\alpha'$ , there is generically an exponentially growing (Hagedorn) density of winding strings as a function of their mass. As space shrinks in the approach

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<sup>2</sup>One of the major developments of recent years being the proof of the Poincaré conjecture by mathematicians, using some techniques from physics.

<sup>3</sup>Inflation stretches  $\mathcal{M}_3$  exponentially, but the interesting logical possibility that its topology is accessible just within our horizon has been studied and bounded, e.g. in [37].



toward the singularity, these states, among others, become important to the dynamics, and they enhance the effective dimension of the system, as follows. In string theory in flat space, there is an exponential density of states arising from oscillations of the strings in the dimensions on which they propagate; for larger dimensionality, the density of states grows more rapidly. More generally, one can extract the effective dimension (or “effective central charge”) from the high-energy density of states in any perturbative string background [38]. At large but finite radius, this Hagedorn density of winding strings on  $\mathcal{M}_3$  leads to a calculable enhancement to the effective central charge, precisely consistent with modular invariance, indicating a supercritical string spectrum in the approach to the singularity [39, 40]. This raises the question of what happens at smaller radius, for example in the window where string  $\alpha'$  effects become important but  $g_s$  is still small.

Let us begin with the case where spacetime fermions have periodic boundary conditions around the  $b_1$  homology one-cycles in  $\mathcal{M}_3$ . In a particular controlled limit one can show that the minimal possible completion within perturbative string theory, preserving the symmetries of the system, is a  $b_1$ -dimensional torus [39]. In other words, a rudimentary study of generic cosmological spacetimes in string theory reveals a novel form of string duality (dubbed D-duality): new dimensions emerge from topology. This provides simple, well-motivated examples in which the effective central charge decreases from a supercritical value to the critical dimension – the final stages of the transition proceeding simply by Hubble expansion, which reduces the effective central charge by decreasing the contribution of the semiclassical winding strings. This establishes, in a regime with a well-controlled expansion in both  $\alpha'$  and the string coupling, that the supercritical string is dynamically closely connected to the critical limits of string theory. Recent progress in the works [41] links highly supercritical and critical corners of string theory, using very useful new techniques involving tachyon condensation along a lightlike surface – a special configuration which affords exact control of  $\alpha'$  effects and can be applied to connect many disparate limits of string theory. We will discuss the generic higher-dimensional phases of string theory further in §5.2.

In the above cases, the string coupling ultimately grows large, and a nonperturbative formulation is required. However, perturbative string theory can sometimes be tractable and self-consistent on sufficiently simple spaces. Many works, e.g. [42, 43, 28, 44, 45], have analyzed spacetime singularities in time-dependent backgrounds involving circles with periodic boundary conditions for fermions, in order to check if this analysis can be self-consistent, and if so to check whether string theory yields a smooth crunch-bang transition. A basic challenge is to control the blueshifting of modes, whose energy density tends to approach the Planck scale as the singularity is approached; these can change the character of the singularity, for example rendering it spacelike rather than lightlike [46]. Earlier work using worldsheet conformal field theory techniques can be found, for example, in [47] (where the spatial slice is an  $S^3$ ).

A class of examples in which winding string physics intervenes to smooth out the singularity before the blueshifting modes reach the Planck scale is obtained by considering one-cycles about which spacetime fermions have *antiperiodic* boundary conditions – and which shrink slowly, in string units, as the space reaches the string scale in size:  $H = \frac{\dot{a}}{a} \ll \frac{1}{l_s}$ . A simple example of this in two dimensions is the Milne spacetime  $ds^2 = -dt^2 + v^2 t^2 d\theta^2$  with  $v \ll 1 \Rightarrow \frac{\dot{a}}{a}|_{vt=l_s} = \frac{v}{l_s} \ll \frac{1}{l_s}$ .

In this situation, the spectrum of strings can be reliably computed and includes a mode that becomes tachyonic as the circle circumference diminishes to the string length. The mass-squared of the lightest strings wound around a circle in  $\mathcal{M}_3$  is

$$m^2 \sim \frac{L(t)^2}{l_s^4} - \frac{1}{l_s^2} + \mathcal{O}(H^2) \quad (2.3)$$

where  $L(t)$  is the proper length of the string and the second term comes from the negative Casimir energy on the string worldsheet. This state becomes a *winding tachyon*  $T$  for  $L(t) < l_s$ , and the condensation of this mode drives the system in a different direction from the singularity predicted by general relativity [48]. At weak string coupling, this effect arises parametrically far from the regime of Planck-scale physics, since the circle is of size  $l_s \sim l_{pl}/g_s \gg l_{pl}$  (where  $l_{pl}$  is the Planck length), and  $H$  is parametrically small compared to the string scale.

This condensate produces a spacetime mass term in the sigma model for strings propagating on this spacetime [49], proportional to a relevant operator in the spatial directions of the worldsheet sigma model. This suggests that the tachyon effectively masses up all the degrees of freedom of the system. This intuition is borne out by calculations of the leading time-dependent effects in the system, made using the “in vacuum” in the tachyon phase. Namely, the particle production read off from the two-point function is exactly the same as in a field-theoretic system with exponentially growing mass, and the one-loop vacuum energy gets contributions only in the region of spacetime in which the tachyon has not condensed. This scenario therefore yields a perturbative string mechanism for an old idea in Euclidean quantum gravity – that of starting time from “nothing”. The tachyon dynamics is quite subtle; one open question concerns the set of allowed states and how to formulate the worldsheet theory appropriate to states other than the in vacuum.

### 2.3 Nonperturbative formulations and the singularity

In many cases, such as rapidly shrinking spaces and spaces with periodic boundary conditions for fermions, nonperturbative effects may ultimately be required to resolve the singularity. It is possible to formulate string theory nonperturbatively in various special spacetime backgrounds, using matrix theory [50] or the AdS/CFT correspondence [51].

These formulations are not well-adapted to cosmology as it stands,<sup>4</sup> but can be used to gain insight into some null and spacelike singularities. Investigations along these lines have suggested methods for calculating effects of the singularity from the gauge theory side [52, 53, 54, 55] and in some cases yield a set of free Yang-Mills degrees of freedom associated with the singularity [56, 57, 39].

### 3 Inflation in Field Theory and String Theory

Although string theory is most directly relevant in the extreme conditions near the initial singularity, inflation, if it occurred, is very effective at screening this microphysics from observation. However, traces of the inflationary epoch itself do remain accessible, and may be our best hope to probe physics at very high energies. Let us therefore turn to inflationary model building and its interface with string theory.

#### 3.1 Inflation in quantum field theory

Inflation provides a solution to several cosmological problems within the realm of effective field theory. We will consider Lagrangians of the fairly general form [58]

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2} M_{pl}^2 \mathcal{R} + P(X^{IJ}, \phi^J) \right], \quad (3.4)$$

where  $\phi_I$  are scalar fields including the inflaton field,  $X^{IJ} = -\frac{1}{2} g^{\mu\nu} \partial_\mu \phi^I \partial_\nu \phi^J$ , and  $P$  is some function. The reduced Planck mass is  $M_{pl} = (8\pi G)^{-\frac{1}{2}}$ .

Two familiar special cases are the two-derivative action for a general curved field space, with

$$P_{SR} = -G_{IJ} \partial \phi^I \partial \phi^J - V(\phi) \quad (3.5)$$

for some metric  $G_{IJ}(\phi^K)$ , and the DBI action

$$P_{DBI} = -f(\phi)^{-1} \sqrt{1 + f(\phi) (\partial \phi)^2} - V(\phi) \quad (3.6)$$

where  $(\partial \phi)^2 \equiv g^{\mu\nu} \partial_\mu \phi \partial_\nu \phi$ , and we have suppressed the  $I, J$  indices. Here  $f(\phi)$  is a function that, although computable in concrete string theory constructions, may be taken to be general for the present purpose. Each of these actions is valid in the limited regime in which all neglected operators, evaluated on the solution of interest, are subdominant to the terms listed. The question of what terms dominate can be quite subtle and sensitive

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<sup>4</sup>AdS/CFT requires a timelike boundary, while Matrix Theory is based on graviton scattering in flat spacetime, and has not been generalized to the case of compactification down to four-dimensional target spaces.

to the details of the UV completion, and this is the source of some of the difficulty, and utility, of embedding these scenarios into string theory. (An effective field theory treatment appropriate to expansion about inflating backgrounds was developed very recently in [59].)

We consider approximately homogeneous and isotropic solutions given by the Friedmann-Robertson-Walker metric

$$ds^2 = -dt^2 + a^2(t)dx_3^2 . \quad (3.7)$$

The Hubble expansion is characterized by  $H = \frac{\dot{a}}{a}$  and is determined by the sources of stress-energy via the Friedmann equations. The stress-energy tensor arising from rolling scalar fields governed by (3.4) has pressure  $P(X, \phi)$  and energy density

$$\rho = 2XP_{,X} - P , \quad (3.8)$$

where  $P_{,X}$  denotes the derivative with respect to  $X$ .

Much recent work has focused on embedding slow roll inflation, an extensively studied mechanism for inflation in quantum field theory based on the two-derivative action, into string theory. At the same time, string theory – in particular the dynamics of scalar fields in AdS/CFT dual pairs – has led to the development of a new field-theoretic mechanism for inflation, obtained from the effective action (3.6). The resulting DBI inflation scenario would benefit from an explicit UV completion, and work continues in this direction. We will discuss progress toward constructions along both these lines in §4.

In any known field-theoretic mechanism for inflation, some fine-tuning of Lagrangian parameters is required. That is, the effective action (3.4) must be chosen carefully to arrange for a long period of inflation producing a suitable spectrum of density perturbations; natural, generic values for these data do not imply a solution of the Big Bang problems. One of the more conservative goals of the subject is to determine explicitly how to implement this tuning in a UV-complete framework, or, conceivably, to discover correlations in couplings that might descend from a full theory even if they appear tuned in the IR theory.<sup>5</sup>

Specifically, one can define (generalized) slow variation parameters whose smallness ensures an extended period of inflation (discussed e.g. in [61]) as follows:

$$\begin{aligned} \epsilon &= -\frac{\dot{H}}{H^2} = \frac{XP_{,X}}{M_{pl}^2 H^2} , \\ \tilde{\eta} &= \frac{\dot{\epsilon}}{\epsilon H} , \\ s &= \frac{\dot{c}_s}{c_s H} , \end{aligned} \quad (3.9)$$

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<sup>5</sup>See [60] for a recent attempt along these lines in the specific context of D-brane inflation.

where the sound speed  $c_s$  is given by

$$c_s^2 = \frac{dP}{d\rho} = \frac{P_{,X}}{P_{,X} + 2XP_{,XX}}. \quad (3.10)$$

In the case of slow roll inflation (3.5), one ensures slow variation by choosing an appropriately tuned flat potential  $V(\phi)$  which one must control (along with the rest of the action) over a sufficient range in field space. In the case of DBI inflation (3.6), the slow motion of the canonically normalized scalar field is ensured by the “speed limit” enforced by the square root action, ensuring that  $\dot{\phi}^2 < 1/f(\phi)$  regardless of  $V(\phi)$ ; one must choose an appropriately tuned  $f(\phi)$  and control it (along with the rest of the action) over a sufficient range in field space.

The Gaussian approximation to the scalar power spectrum derived from the two-point function is given by [58]

$$\mathcal{P}_k^\zeta = \frac{1}{8\pi^2 M_{pl}^2} \frac{H^2}{c_s \epsilon}, \quad (3.11)$$

where the expression is evaluated at the time of horizon exit at  $c_s k = aH$ . Observations give  $\mathcal{P}_k^\zeta \approx 10^{-9}$ . The spectral index is

$$n_s - 1 = \frac{d \ln \mathcal{P}_k^\zeta}{d \ln k} = -2\epsilon - \tilde{\eta} - s. \quad (3.12)$$

The power in tensor perturbations at the Gaussian level is

$$\mathcal{P}_k^h = \frac{2}{\pi^2} \frac{H^2}{M_{pl}^2}. \quad (3.13)$$

The tilt and tensor-to-scalar ratio  $r = \mathcal{P}_h/\mathcal{P}^\zeta$  are bounded such that  $n_s \sim 0.95$  at  $r \sim 0$  while larger  $r$  correlates with the possibility of larger  $n_s$  [2].

The possibility of detecting gravitational waves from inflation [62] is in fact an example of a question which is very sensitive to UV physics. Lyth has shown that a detectable gravitational wave signal requires a super-Planckian field range for the canonically normalized inflaton field [63]. This extends to more general theories of the form (3.4) [64]. Arranging for the slow variation parameters (3.9) to be small over such a range is extremely delicate: corrections  $\mathcal{O}_\Delta/M_{pl}^{\Delta-4}$  to the effective action involving higher dimension operators  $\mathcal{O}_\Delta$  of dimension  $\Delta > 4$  generically become important if the inflaton ranges over a Planck-scale (or higher) range in field space. Moreover, in most controlled backgrounds of string theory there are degrees of freedom at a lower scale than  $M_{pl}$ , leading to larger effects that interfere with inflation even over sub-Planckian field ranges.

The Lagrangian (3.4) contains higher-point interactions of the perturbations of  $\phi$  and the graviton. Therefore there is a non-Gaussian correction to the power spectrum. In single-field

slow roll inflation, the leading such effect includes couplings to gravitons and is unmeasurably small (see [33]). The inclusion of higher-dimension operators suppressed by a high mass scale as in [65] improves the prospects somewhat. Building on this, more generically one obtains higher-dimension operators suppressed not by a hard mass parameter, but instead by the inflaton vev itself,  $\phi$  [66]. In this circumstance the non-Gaussian correction can be substantial [67]. As an example, in DBI inflation (3.6), expanding in perturbations about the background solution brings down powers of  $\gamma = 1/\sqrt{1 - f\dot{\phi}^2}$ , which is large in the solution when  $\dot{\phi}$  approaches its speed limit. This correction is large enough to ensure that the DBI inflation mechanism is falsifiable: its entire parameter range will be covered by upcoming experiments.<sup>6</sup> The non-Gaussian correction to the power spectrum has been computed in general single-field inflation in [61] following [33, 65, 67]; an effective field theory treatment appears in [59, 68]. To first order in the slow variation parameters, the three-point function for the gauge-invariant scalar perturbation  $\zeta$  is of the form

$$\begin{aligned} \langle \zeta(\mathbf{k}_1)\zeta(\mathbf{k}_2)\zeta(\mathbf{k}_3) \rangle &= (2\pi)^7 \delta^3(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{k}_3) (\tilde{\mathcal{P}}_k^\zeta)^2 \frac{1}{\prod_i k_i^3} \\ &\times (\mathcal{A}_\lambda + \mathcal{A}_c + \mathcal{A}_o + \mathcal{A}_\epsilon + \mathcal{A}_\eta + \mathcal{A}_s) . \end{aligned} \quad (3.14)$$

The shape decomposes into the six functions  $\mathcal{A}_I, I = 1, \dots, 6$  given in Appendix B1 of [61]. Large non-Gaussianity is correlated with small sound speed; in DBI inflation  $c_s \sim 1/\gamma$ .

Non-Gaussian corrections have been bounded by the WMAP data [2][69]. The three-point function (3.14) depends on two independent momentum vectors, or equivalently on a triangle in momentum space. The amplitude of the effect as a function of momentum triangles depends on the model; for DBI inflation the WMAP data currently bounds  $\gamma \lesssim 20$ , for example. There are currently investigations into other observational methods to bound (or detect) primordial non-Gaussianity.

Some authors have explored the question of whether there is a nontrivial choice of vacuum for the scalar perturbations (deviating from the Bunch-Davies vacuum assumed above), and if so how this would affect the power spectrum (see for example [70, 71, 72]). The conservative view seems to be that an initial excitation above the Bunch-Davies vacuum would thermalize during inflation, reducing the system back to Bunch-Davies; however, even given this there is a chance that initial transients appear within the CMB window of observability. A nonstandard choice of vacuum endows (3.11) with a momentum-dependent prefactor which can be bounded by observations.

In addition to probes of and constraints on inflation from the power spectrum, there are observational constraints and opportunities from relics such as cosmic strings produced in the exit from inflation. We will not cover this in detail since it has been reviewed very

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<sup>6</sup>This statement is based on the original predictions of the sensitivity of the Planck satellite, for example, which may be revised downward.

recently in [73, 74, 75]. In the context of string theory, the gravitational redshift (warping) used in the scenarios of [76] (§4.2) to obtain inflation with suitably small  $\mathcal{P}_k^\zeta$  has the added effect of redshifting down the string tension in D-brane inflation [77] to a viable scale [78]. This excess of outputs over inputs is one of the encouraging signs in the subject as developed thus far. The cosmic superstrings arising in this context have a rather rich phenomenology [79]. An important step was made in realizing that cusps and kinks on cosmic strings lead to a distinctive gravity wave signature [80].

## 3.2 Challenges for inflation in string theory

The primary task in string inflation is to specify a string compactification whose low-energy effective Lagrangian is capable of producing inflation that is consistent with current observations. This turns out to be a surprisingly difficult problem, and there is no definitive proof of a *fully* successful model at the time of this writing. Once this has been achieved, one can search for special features of the string-derived Lagrangian that might provide characteristic signatures of the model. In this section we will explain the obstacles to success, and in the next section we will describe a range of relatively successful models. Of course, as discussed already, string theory also contributes to the development of inflation at the field-theoretic level by inspiring new mechanisms and models, some of which are testable independently of their UV completion.

### 3.2.1 From compactification data to the inflaton Lagrangian

In principle, one would like to construct a string inflation model by specifying the data of a consistent string compactification, including the total dimensionality; the geometry and topology (or generalization thereof)<sup>7</sup>; the locations of any D-branes, orientifold planes, and other localized sources; and the amount of flux turned on through each cycle. Such a configuration would uniquely specify a four-dimensional classical Lagrangian, and our knowledge of this theory would be limited only by the accuracy of the dimensional reduction – for example, by  $\alpha'$  and  $g_s$  corrections, or by backreaction effects from the localized sources.<sup>8</sup>

At present, however, most models are constructed less directly, through a certain amount of informed guesswork. For example, moduli stabilization is most often accomplished by invoking a general method, such as the proposal [9, 12], instead of by a precise specification

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<sup>7</sup>Although here we will focus mostly on geometric backgrounds, various authors have emphasized the possible genericity of non-geometrical ones [81], and indeed early landscape models made use of asymmetric orbifolding, and hence were of this more general type [10, 11].

<sup>8</sup>Of course, the quantum-corrected value of the cosmological constant cannot be computed in this setup, and in any framework for modeling the real-world dark energy, a genericity argument is used to argue that the quantum corrections can be cancelled by appropriate tuning of discrete quantum numbers.

of fluxes and perturbative and nonperturbative effects; ingredients responsible for tadpole cancellation, such as orientifold planes, are assumed to be so far away from the region where the inflation effect is localized that they have no effect on the potential; the metric on a noncompact cone is sometimes used as an approximation to that of a finite conical region in a compact space; and very often  $g_s$  and  $\alpha'$  corrections are omitted without sufficient concern for their effects on the putative inflationary solution.

In many cases, these approximate treatments are the best that can be accomplished with present knowledge. Approximations of this sort suffice only as long as they do not lead to important inaccuracies, which in the worst case can cause a model to appear successful at leading order but to fail totally when corrections are included. Although at present no entirely systematic method exists for estimating the errors in all these approximations, we will present, in §3.2.2, a useful scheme for organizing corrections to the leading-order dimensional reduction. This helps to identify cases in which a model is in jeopardy and computation of higher corrections is necessary. To justify the scheme, however, we first explain two general and important obstacles in string inflation model-building: the moduli problem and the eta problem.

### 3.2.2 *The moduli problem and the eta problem*

The first difficulty is that string compactifications invariably involve more than one scalar field, and so are much more complicated than the single-field Lagrangians of the preceding section. The four-dimensional potential depends, in general, on all the moduli of the compactification, which parametrize the geometry of the internal space. In Calabi-Yau compactifications, one has Kähler moduli, complex structure moduli, and the dilaton, numbering in the hundreds in typical cases. Computing the full potential as a function of all these fields is a formidable task, and even if one could succeed, it would then be necessary to search through the high-dimensional field space for a path along which the resulting potential<sup>9</sup> is sufficiently flat for inflation.

An essential point is that it does *not* suffice to hold fixed, by hand, all fields but one, and then find a path along which the potential for that single field,  $\phi_1$ , is flat. One reason is that the full potential will typically have a steep downhill direction coinciding with one or more of these other fields,  $\phi_2, \dots, \phi_N$ . If the steepest such direction is more steep than the desired, and nearly flat, inflaton direction, the full system will evolve by rolling downhill in this steepest direction rather than along the putative inflaton direction  $\phi_1$ . Thus, one must actually arrange that the potential has positive curvature in the directions of  $\phi_2, \dots, \phi_N$ .

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<sup>9</sup>For simplicity of exposition, we focus here on realizing slow roll inflation, but the issues are analogous for more general models, in which the potential need not be flat but other operators in the action are constrained by the need for small generalized slow roll parameters (3.9).



This, too, is not sufficient: a field  $\chi$  with  $0 < m_\chi^2 < \frac{3}{2}H^2$  will undergo quantum fluctuations during inflation. These fluctuations carry the field away from its minimum and hence lead to storage of energy in  $\chi$ . If  $\chi$  is quite light and couples only gravitationally (as moduli do), the  $\chi$  particles will not have decayed by the present day, and will overclose the universe. If  $\chi$  is somewhat heavier, up to  $\sim 30$  TeV, it will have decayed during or after Big Bang Nucleosynthesis, spoiling the delicate predictions of the light element abundances. To avoid this ‘cosmological moduli problem’, one must<sup>10</sup> therefore arrange that  $m_\chi^2 > 30$  TeV, and preferably that  $m_\chi^2 \gg H^2$ . Giving moduli large positive masses is known as moduli stabilization.

Explicit techniques that stabilize most or all of the compactification moduli became available only in the last decade. An approach pursued in the absence of moduli stabilization was to assume that whatever mechanism stabilizes the moduli does not affect the inflaton potential. This turns out *not* to be a valid assumption. One qualitative reason to expect a problem is that moduli stabilization aims to arrange  $m_{\chi_i}^2 \gg H^2$  for all the runaway moduli  $\chi_i$ ,<sup>11</sup> whereas inflation requires  $m_\phi^2 \ll H^2$ . Since the inflaton is usually nothing more than a carefully-chosen modulus, the origin of this sharp disparity is hard to justify: whatever mechanism lifts the flat directions of all the other moduli potentials will also lift the inflaton flat direction. This expectation has now been established in a wide range of examples, and is in fact a specific incarnation of a more general difficulty known as the eta problem.

We first recall that from the definition of the slow roll parameter  $\eta$ ,

$$\eta \equiv M_{pl}^2 \frac{V''}{V}, \quad (3.15)$$

with primes denoting derivatives with respect to an inflaton  $\varphi$  with a canonical kinetic term, we have  $m_\varphi^2 = \frac{V}{M_{pl}^2} \eta = 3H^2 \eta$ . Hence, the inflaton mass being of order  $H$  is equivalent to having  $\eta \sim 1$ . Moreover, as  $\eta$  governs the duration of slow roll inflation,  $\eta \sim 1$  leads to an unacceptably small amount of inflation.

The eta problem is the observation that, in string theory and effective field theory realizations of inflation (including supersymmetric ones), Planck-suppressed corrections to an otherwise flat inflaton potential generically give rise to inflaton mass terms of order  $H$ , leading to  $\eta \sim 1$ , and hence ruining slow roll [83]. Specifically, Planck-suppressed contributions to the potential of the form

$$\Delta V = \frac{\mathcal{O}_4}{M_{pl}^2} \phi^2, \quad (3.16)$$

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<sup>10</sup>Axions with sufficiently small periodicity can be viable below this bound, as their potential energy and initial displacement from their minimum are smaller than for generic moduli; see [82] for a recent discussion of the constraints on axions and a survey of their parameters in a sample of string backgrounds.

<sup>11</sup>It is possible for moduli other than the inflaton to have lighter masses, as long as they sit at a local minimum during inflation and as long as they sit at or roll toward a stable minimum at the end of inflation.

for some operator  $\mathcal{O}_4$  of dimension four, lead to mass terms

$$\Delta m_\phi^2 \propto \frac{\langle \mathcal{O}_4 \rangle}{M_{pl}^2}. \quad (3.17)$$

Then, if  $\langle \mathcal{O}_4 \rangle \sim V$ , these contributions lead to  $\Delta\eta \sim 1$ .

In the context of models with a low-energy supergravity description, the most transparent contribution of this sort is present whenever there is an F-term energy of order the inflationary energy. This condition is obviously met when inflation is driven by an F-term, but is also typically obeyed when moduli stabilization is accomplished via an F-term. The intuitive reason for this is that a small moduli-stabilizing energy cannot prevent a large inflationary energy from driving a runaway decompactification, so what is often obliged to consider moduli-stabilizing energies of order the inflationary energy.<sup>12</sup> In any such case, in terms of the Kähler potential  $K$  and superpotential  $W$ , we have

$$V \approx V_F = e^{K/M_{pl}^2} \left( K^{A\bar{B}} D_A W D_{\bar{B}} \bar{W} - \frac{3}{M_{pl}^2} |W|^2 \right) \quad (3.18)$$

Next, we expand  $K$  around some fiducial origin  $\phi = 0$  as  $K = K(0) + K_{,\phi\bar{\phi}}(0)\phi\bar{\phi} + \dots$  and find, for small  $\phi$ ,

$$\mathcal{L} \approx -K_{,\phi\bar{\phi}} \partial\phi \partial\bar{\phi} - e^{K(0)/M_{pl}^2} \left( 1 + \frac{1}{M_{pl}^2} K_{,\phi\bar{\phi}} \phi\bar{\phi} \right) \left( K^{A\bar{B}} D_A W D_{\bar{B}} \bar{W} - \frac{3}{M_{pl}^2} |W|^2 \right) + \dots \quad (3.19)$$

Noting that the canonically-normalized inflaton  $\varphi$  obeys  $\partial\varphi\partial\bar{\varphi} \approx K_{,\phi\bar{\phi}}(0)\partial\phi\partial\bar{\phi}$ , we see that the contribution to the mass term of  $\varphi$  is  $\Delta m_\varphi^2 \approx V_F(0)/M_{pl}^2 = 3H^2$ , so that  $\Delta\eta = 1$ . In (3.19) we have indicated explicitly only the terms arising from the expansion of the exponential; the ellipsis stands in part for terms arising from expanding the factor in brackets in (3.18). These latter terms give contributions to  $\eta$  of comparable size to those we display, but are more model-dependent.<sup>13</sup>

More generally, the eta problem will arise whenever a term in the potential of order  $V$  is corrected multiplicatively by a generic function of  $\phi/M_{pl}$ . For example, the nonperturbative superpotential used for Kähler moduli stabilization in the KKLT scenario receives a multiplicative correction depending on the positions of any D3-branes [84, 85, 86, 87]. In D3-brane inflation, this gives rise to a contribution  $\Delta\eta \sim 1$  [76, 85, 88, 60], because, as mentioned above, the moduli-stabilizing energy is generically of the same order as the inflationary energy.

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<sup>12</sup>This relation could be violated by an unusually steep moduli-stabilizing potential.

<sup>13</sup>For example, in the scenario of [76], expanding  $K$  everywhere it appears in (3.18), not just in the exponential, one finds  $\Delta\eta = 2/3$ .

An instructive way to organize corrections to the inflaton Lagrangian is in terms of the scale of the masses (or other derivatives of the potential) they generate. First, we denote by  $\mathcal{L}_0$  the leading-order Lagrangian arising from dimensional reduction. Next,  $\mathcal{L}_1$  is defined to include all corrections to  $\mathcal{L}_0$  that introduce inflaton mass terms that are parametrically  $\Delta m^2 \sim H^2$ . Finally,  $\mathcal{L}_2$  contains all corrections that introduce inflaton mass terms that are parametrically smaller than  $\Delta m^2 \sim H^2$ , e.g.  $\Delta m^2 \sim g_s H^2$  and the like. In this language, merely to recognize the presence of the eta problem, one must have some information about terms in  $\mathcal{L}_1$ ; to be certain that the problem is solved and the inflaton potential is very flat, one needs comprehensive information about  $\mathcal{L}_2$ .

In some cases, there is a concrete framework for computing these Planck-suppressed contributions to the potential. In  $\mathcal{N} = 1$  supergravity, these corrections more often appear in the Kähler potential than in the superpotential, because the latter is protected by holomorphy. String loop and  $\alpha'$  corrections to the Kähler potential then lead to the relevant terms in  $\mathcal{L}_1$  and  $\mathcal{L}_2$ . Unfortunately, computing these terms, especially those in  $\mathcal{L}_2$ , is extremely difficult and has only been undertaken by a few authors [89].

In the absence of such information, appeals to fine-tuning are sometimes made: one argues that in some restricted subset of possible models, the net correction might be accidentally small. The typical argument is that the terms in  $\mathcal{L}_1$  are not small, but happen to cancel each other to high precision for fine-tuned values of the microphysical parameters. This is an expectation, and has not been rigorously justified in most cases. In fact, a reasonably comprehensive examination [88, 60] of the terms in  $\mathcal{L}_1$  for models of warped D-brane inflation has revealed that fine-tuning itself is possible only in a very restricted subset of compactifications; in particular, there exist compactifications in which all the terms in  $\mathcal{L}_1$  have the same sign.

Although the eta problem is well-known, one often encounters spurious claims that a given model of string inflation is free of fine-tuning, when in fact it is simply the case that the potential has not yet been computed with enough accuracy to ascertain whether the problem is present or not! (Let us emphasize that we are not suggesting that all such claims are incorrect in this way, only that many are.)

Another proposed solution to the eta problem is to include protective symmetries. Although well-motivated, this approach has been surprisingly difficult to achieve in explicit models, because the desired symmetries do not always survive quantum corrections.

At present, the eta problem is one of the most serious constraints limiting our ability to construct explicit models of string inflation.

### 3.2.3 Constraints on field ranges

In a few models of inflation, the inflaton traverses a distance in field space that is large compared to the Planck mass. This category includes some of the scenarios which are simplest from the point of view of their field content, such as Linde’s chaotic inflation with a quadratic potential. It also includes all models that produce a detectably-large primordial tensor signal: as explained by Lyth, inflaton motion over a Planckian distance is a necessary condition for such a signal.

To realize any such ‘large-field’ [90] model in string theory, one would need to find a trajectory in field space that is large in Planck units, and along which the effective action (3.4) is suitable for inflation. This has proved to be very difficult. One way to anticipate this problem in the case of models with a low-energy supergravity description is to write the possible corrections to the Kähler potential,

$$\mathcal{K} = \mathcal{K}_{\text{classical}}(\Phi, \Phi^\dagger) + M_{\text{pl}}^2 \sum_i c_i \left( \frac{\Phi \Phi^\dagger}{M_{\text{pl}}^2} \right)^{1+i} \quad (3.20)$$

where the dimensionless coefficients  $c_i$  may be true constants or may depend on other fields in the system. Unless the  $c_i$  are all very small, this series is badly divergent for  $\Phi \gg M_{\text{pl}}$ , and so over Planckian distances, the metric on moduli space is poorly-described by the classical metric on moduli space derived from  $\mathcal{K}_{\text{classical}}$ . More generally, similar comments apply to the quantum-corrected effective action in cases without a low-energy SUSY description in terms of a Kähler potential.

An exception arises near weak-coupling limits of string compactifications, which go off to infinite distance in moduli space. Here, the weak coupling allows one to calculate the effective action to a good approximation. At least in the simplest examples yet studied, the result is an exponential potential in the canonically normalized scalar fields, with a coefficient in the exponent which is of order one, too steep for slow roll inflation. However, we are not aware of a sharp no-go theorem for inflation at this level, in the generally rather complicated context of arbitrary compactification manifolds with many scalar fields; it would be interesting to understand if there is a principled obstruction to inflation in tree-level string theory. Conversely, away from weak coupling it is difficult to assert with confidence that one knows that the size of a given moduli space is large in Planck units.

In certain specific contexts in string theory, we can compute the field ranges more explicitly, in regimes appropriate to candidate inflation models. An example of this is the field range for a D3-brane in a warped throat region, a topic we will review in the next section. As shown in [91], for any sort of warped throat arising from a cone over an Einstein manifold, the field range in Planck units is small. Similar bounds are easily derived for D3-branes moving in (most) toroidal compactifications. This result implies that D3-brane inflation in

Calabi-Yau throats, or in most tori, cannot give rise to an observably-large primordial tensor signal.

Of course, nothing a priori requires D3-branes, and as explained very recently in [92], one interesting way to evade this constraint is to develop an inflationary scenario involving the motion of a  $D(p+3)$ -brane wrapped on a  $p$ -cycle, for  $p > 0$ . In such a case the relation between the geometric distance and the physical canonical field is different than in the D3-brane case, and larger canonical field ranges are possible [92]. It is worth noting that in special compactifications, D3-branes *are* advantageous in the case of slow roll inflation (described below in §4.2.1) since their potential is flat at leading order by a generalization of no-scale structure. In the case of DBI inflation (described below in §4.2.2), a steep potential is useful, so the higher-dimensional branes may be practical in this case.

In closed string models, the field ranges correspond to distances in the space of geometric moduli, not distances in the compactification itself. An example of the situation discussed above of an infinite direction in the moduli space is the decompactification direction. In the case of low-energy supergravity, one parameterizes this in terms of the Kähler potential and superpotential. The Kähler potential depends on the total volume  $\mathcal{V}$  as

$$\mathcal{K} = -2M_{pl}^2 \log(\mathcal{V}) , \quad (3.21)$$

so that  $R \equiv M_{pl}\sqrt{2} \log(\mathcal{V})$  has a canonical kinetic term. The range of  $R$  between any fixed  $\mathcal{V} \sim \mathcal{V}_0$  and the limiting point  $\mathcal{V} \rightarrow \infty$  is arbitrarily large. This would seem to be a promising setting for large-field inflation, but it remains difficult to find a suitable inflaton potential along this direction. The problem is related to the logarithmic form of the Kähler potential: energy sources that have power-law dependence on  $\mathcal{V}$  depend exponentially on the canonical field  $R$  – with a Planck-scale coefficient in the exponent – causing the potential to vary rapidly along the  $R$  direction.

An interesting approach to constructing a microphysically-sensible super-Planckian vev was presented in [93]. By combining the displacements of  $N \gg 1$  string axions into an effective displacement of a collective field, these authors sidestepped the above restriction on individual field ranges. However, important questions remain about the radiative stability of this scenario, as we review in §4.4.2.

Most successful closed string models involve potentials that are flat over very small ranges of the canonical inflaton. Such ‘small-field’ models typically require fine-tuning and can be highly sensitive to initial conditions, but they have the advantage that physics associated with Planckian displacements plays no role.

Notice that models with small field ranges, and hence [63] lower tensor signals, also have lower Hubble scales during inflation, because the tensor signal (3.13) is proportional to  $H^2$ . In order for inflation to set in, a smooth patch of linear size  $H^{-1}$  is required. Thus, small-field models require smoother initial patches than large-field models require; on the

other hand, large-field models require *functional* fine-tuning in the effective action in order to allow for inflation over a super-Planckian field range. It would be interesting to understand whether the functional fine-tuning in large-field models is counterbalanced by the necessity of smoother initial patches in small-field models. This question is, in turn, sensitive to earlier physics, including questions about probability measures from eternal inflation.

Another interesting, and rather strong, and constraint on the tensor signal in certain classes of string compactifications is [94].

## 4 Models of Inflation in String Theory

As we have discussed, proposing a model of inflation in string theory typically amounts to describing the data of a compactification whose low-energy effective theory can contain a suitable inflaton field. One often requires as well that there is a plausible mechanism for reheating the universe. The most potentially exciting models are those with novel and distinctive signatures, but this is not a requirement by any means: it remains worthwhile to construct definitively successful models of string inflation, even if these happen to lack striking observational signatures, for precisely the same reason that is worthwhile to find string constructions of the Standard Model of particle physics.

Because proposing a model involves identifying a scalar field as an inflaton candidate, we can classify string inflation models according to the origin of the inflaton field. Open-string models, usually called D-brane inflation or brane inflation models, are those in which the inflaton is a scalar field arising from open strings ending on a D-brane; some of the original papers on this approach are [95, 96, 97, 98, 99, 100]. Usually this scalar parameterizes transverse motion of the D-brane, and hence governs the location of the D-brane in the compactification. In M-theory, there is a closely-related alternative in which the inflaton corresponds to the position of an M5-brane.

Closed string models are those in which the inflaton is a closed string mode. The moduli are the most promising closed string modes, as there is a well-defined choice of background for which a subset of them enjoy classically flat potentials. (Of course, this does involve a special choice of starting point; the *generic* classical potential for moduli of the metric and  $p$ -form fields is too steep for inflation.) For this reason, closed string inflation is sometimes called moduli inflation or modular inflation. Classic works in this framework include [101].

Because of limitations of space, we will not attempt to present a large fraction of current models here. Instead, we will describe a few characteristic models in each category. We do not mean to imply that the scenarios selected are the most promising or most interesting among extant models; however, in our judgement they are *representative* of the leading edge of contact between inflation and concrete string theory data.

It should be emphasized that any particular concrete model – in field theory or in string theory – is based on specific, perhaps improbable, choices of microscopic ingredients and field content which are not forced upon us directly by the data. Nevertheless, it seems to us that investigations of this sort offer a surprising degree of insight into important classes of behavior in string theory. Moreover, models of the present generation have led to a range of novel and genuinely predictive possibilities for inflation within quantum field theory.

## 4.1 D-brane inflation

D-brane inflation has been the subject of much recent work, and the result is a wide array of scenarios. At present D-brane models are best-studied in type IIB string theory, due in part to the comparatively better understanding of moduli stabilization in the type IIB theory.<sup>14</sup> One natural candidate for the inflaton field is the position of a spacetime-filling D3-brane. D3-branes feel no potential, at leading order in  $\alpha'$  and  $g_s$ , in the no-scale flux compactifications of [9]. Thus, the moduli space of a D3-brane in such a compactification is the entire internal space, and one can hope to find a weak additional effect that will slightly lift this moduli space. Examples of such effects include magnetic flux on a D7-brane wrapping a four-cycle [102] (see also [103]), an antibrane at the tip of a Klebanov-Strassler throat [104], and a baryonic branch deformation of the Klebanov-Strassler geometry [105], as well as  $F$ -term energy [106].

One interesting and well-studied proposal is D3-D7 inflation, in which a D3-brane moves towards one or more D7-branes that wrap the  $K3$  of a  $K3 \times T^2 / \mathbb{Z}_2$  compactification (or a more general space) [107]. This is a D-term inflation scenario, but F-term moduli stabilization (for example, by the KKLT method), as well as mixing between the D3-brane moduli and Kähler moduli in the Kähler potential [108], lead to inflaton mass terms, as in [76]. It was proposed [109] that geometric symmetries of the (toroidal part of the) compactification could protect the inflaton potential from these problematic terms. However, one-loop threshold corrections to the nonperturbative superpotential [85] violate this shift symmetry and lead to a reappearance of the eta problem in this context [110]. It would be interesting to understand whether there exists a configuration of the D-branes in this compactification in which the inflaton mass term can be made to cancel. Such a construction would still amount to a fine-tuning, not a natural solution of the eta problem, but would be valuable nonetheless, given the high degree of computability of this model, and the access to explicit information about moduli stabilization [111].

A more general possibility for the inflaton is a  $D(p+3)$ -brane wrapped on a  $p$ -cycle. In such cases, to study the moduli space one needs information about families of  $p$ -cycles,

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<sup>14</sup>For example, the solutions can remain conformally Calabi-Yau even in the presence of flux, which is an important technical advantage.

which is easily obtained in toroidal and constant curvature target spaces, but somewhat more challenging in general compactification manifolds.

Another proposal is to associate the inflaton with the orientation, rather than the center-of-mass position, of a D-brane [112, 113].

Some other interesting ideas, similar in spirit to those presented here, include [114].

## 4.2 Warped D-brane inflation

### 4.2.1 *Slow roll*

The Coulomb interaction between a D3-brane and an anti-D3-brane in a compact region of flat six-dimensional space is generically too steep for inflation. The proposal of [76] is that a brane-antibrane pair separated along a warped region, such as the radial direction of a warped deformed conifold, enjoys a much flatter Coulomb interaction. Geometries of this sort are well-understood: they are well-approximated by non-compact solutions, they fit naturally into the framework of type IIB moduli stabilization with fluxes [9], and a useful everywhere-smooth solution is available, thanks to the work of Klebanov and Strassler [115]. Moreover, strongly warped compactifications allow considerable freedom in choosing energy scales. In particular, it is worth remarking again that as discussed in §3.1, the warped geometry has the added bonus of redshifting down cosmic string tensions, making them a viable and interesting source of potential contact with observations [80, 77, 78].

The warped brane inflation scenario [76] makes use of these important technical advantages, but in the end is still constrained by the eta problem: a brane-antibrane pair separated along a generic warped throat does not give rise to prolonged inflation [76].<sup>15</sup>

A wide variety of solutions to this ‘inflaton mass problem’ have been proposed. In a compactification with a suitable  $\mathbb{Z}_2$  symmetry exchanging two throats, the problem can be absent [119]. Alternatively, as we will review in detail in §4.2.2, the DBI kinetic term of a D3-brane leads to a qualitatively new kind of inflation that does not require a nearly-flat potential, and in some circumstances this mechanism governs the motion of a D3-brane in a warped throat. Another proposal was that a different sort of dynamical effect could flatten the inflaton potential [120]; however, this effect relied on adjusting a parameter that was later found to be zero [87, 121].

Another proposed solution is to incorporate further corrections to the inflaton potential which might, in fine-tuned cases, cancel the problematic inflaton mass term [76]. Such corrections are automatically present: the nonperturbative superpotential of the KKLT scenario

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<sup>15</sup>Much subsequent work has explored the phenomenology of this scenario (see e.g. [116]), and the important question of reheating was considered in [117]. Another proposal for D-brane inflation in a warped throat is [118].



necessarily depends on the D3-brane position [84], and this gives rise to an effective interaction between the D3-brane and the wrapped branes responsible for the nonperturbative superpotential [85, 86, 87].

Without detailed information about the functional form of this contribution to the potential, one could only conjecture that in a certain fraction of cases, the corrected inflaton potential is sufficiently flat. However, this correction was determined in full, for toroidal orientifold cases, via an open string one-loop computation in [85]. Subsequent work in [86] proposed that this computation could also be performed in the closed string channel, and this was accomplished for warped throat backgrounds in [87]. Equipped with this result, one could ask whether the contributions to the inflaton potential indeed cancel for specially-chosen ranges of the microscopic parameters. As shown in [121], this is impossible if the wrapped branes are described by the simple Ouyang embedding [122]. However, it was shown in [88, 60] that if the wrapped branes are described by the simple and symmetric Kuperstein embedding [123], the potential can contain an approximate inflection point at some distance from the tip of the throat. Inflation can occur around this inflection point. (See also [124].)

The resulting scenario is unusually concrete and explicit. Even so, it will still be necessary to determine whether the gluing of the throat region into a compact bulk causes any distortions of the supergravity background that might correct the inflaton potential. In addition, even if such effects are absent, the construction is somewhat delicate: the inflection point is present only for a restricted range of parameters, and the predictions of the scenario, including whether the scalar spectrum is red or blue, depend on fine details of the potential. This is an imperfect state of affairs, and it would be worthwhile to develop a more robust and natural D-brane inflation scenario that can be realized in a concrete compactification.

#### 4.2.2 DBI

As discussed in §2, DBI inflation is a mechanism for slowing the motion of scalar fields via the action (3.6), whose dynamics enforces

$$f(\phi)\dot{\phi}^2 \leq 1 \tag{4.22}$$

regardless of the steepness of the potential.

Given the effective action (3.6), there is a viable window of parameters (functions  $f(\phi)$  and  $V(\phi)$ ) where inflation occurs, and where the density perturbations are consistent with CMB observations. Moreover, model-independently the density perturbations are sufficiently non-Gaussian to be testable by the Planck satellite measurements (and are already constrained by WMAP [2, 69]). As with  $m^2\phi^2$  chaotic inflation, one would like to understand if there is an explicit UV complete model realizing this mechanism.

The DBI mechanism for slowing down the scalar field was originally discovered in the motion on the Coulomb branch of the  $\mathcal{N} = 4$   $U(N)$  SYM theory at large 't Hooft coupling  $\lambda = g_{YM}^2 N \gg 1$ , using the AdS/CFT correspondence. On the gravity side of the correspondence, the rolling of the scalar field  $\phi$  toward the origin of moduli space corresponds to a D3-brane probe moving in the radial direction toward the horizon of the Poincare patch of  $AdS_5$  (and sitting at a point in the  $S^5$ ). This motion is governed by the action (3.6) with warp factor  $f(\phi) = \lambda/(8\pi^3 g_s \phi^4)$  and potential  $V(\phi) = -1/f(\phi)$ . The DBI action enforces the causal speed limit (4.22) on the motion of the probe in the gravity-side description. The brane moves in the  $r = \phi \sqrt{(2\pi)^3 g_s \alpha'^2}$  direction in the space

$$ds^2 = \frac{r^2}{R^2} \eta_{\mu\nu} dx^\mu dx^\nu + \frac{R^2}{r^2} (dr^2 + r^2 d\Omega_5^2) \quad (4.23)$$

where  $R = \sqrt{\alpha'} \lambda^{1/4}$  is the AdS curvature radius. The brane cannot move faster than the speed of light in this background (4.22). Thus, even though the distance to the origin of moduli space  $\phi = 0$  is finite (and uncorrected quantum-mechanically), in the large  $N$  approximation it takes forever to reach the origin [66].

In the CFT language, the reason for this effect is the following. Consider taking one eigenvalue  $\phi$  of the adjoint scalar away from the origin. This breaks  $U(N) \rightarrow U(N-1) \times U(1)$ . The modes  $\chi$  charged under the  $U(1)$  (and in the  $\mathbf{N} - \mathbf{1}$  representation of  $U(N-1)$ ) have mass proportional to  $\phi$ . Since this mass decreases as  $\phi \rightarrow 0$ , the radiative corrections from integrating out the  $\chi$  multiplets generate higher-dimension operators suppressed by powers of  $\phi$  itself (rather than being suppressed by some hard high mass scale  $\Lambda$ ). The first such correction, protected by supersymmetry, is  $f(\phi)(\partial\phi)^4$ . Since the field theory is strongly coupled, it is difficult to sum the series of higher order terms, but the AdS/CFT correspondence allows us to do this, revealing the result to be the DBI action (3.6) (with  $V(\phi) = -1/f(\phi)$ ).

With this new mechanism for slowing scalar field motion in hand, it is natural to embed it into a gravity theory and use  $\phi$  for the inflaton. Formally cutting this theory off, coupling it to gravity, and introducing a more general potential  $V(\phi)$  in (3.6) leads to the DBI mechanism for inflation [66, 67] whose results were reviewed in §2. Recent work [125] has analyzed solutions for a wider space of functions  $f(\phi)$  and  $V(\phi)$ .

One would like to understand if this arises from an explicit string theory model. A first set of attempts to achieve this has been made by taking the field theory mechanism discussed above, and implementing the cutoff and the coupling to four-dimensional gravity by embedding the throat (4.23) in a compact manifold, matching at some scale  $\phi_{UV}$ . Two regimes have been explored in more detail in the literature (the so-called “UV model” with potential of the form  $V(\phi) = m^2 \phi^2$  and Chen’s “IR model” [126] – a small-field hilltop version of DBI inflation with potential of the form  $V(\phi) = V_0 - m^2 \phi^2$ ). Of course these

two specific shapes for  $V(\phi)$  are not particularly important, though they suffice to illustrate some of the relevant features. The  $m^2\phi^2$  model, which entails a Planck-scale field range and detectable gravitational waves, cannot arise from *three*-branes in a Calabi-Yau throat as originally envisioned [91, 127, 128, 129]. The four-dimensional Planck mass  $M_{pl}$  in this setup is given by

$$M_{pl}^2 = \frac{2\pi^3}{(2\pi)^7 g_s^2 \alpha'^4} \int^{r_{UV}} R^4 r dr = \frac{N}{4} \phi_{UV}^2 \quad (4.24)$$

Thus, the field range  $\phi_{UV}$  is parametrically small compared to the Planck mass [91]. This result applies not just to the original  $\text{AdS}_5 \times \text{S}^5$  geometry, but also to any warped throat generated by D3-branes at the singularity of a cone over some Einstein manifold  $X_5$ . However, for wrapped higher-dimensional  $Dp$ -branes rather than D3-branes [92] in a Calabi-Yau or a more general compactification, a Planckian or super-Planckian field range is geometrically possible.

Moreover, a generic model in the landscape has cycles supported by a wider variety of fluxes; moreover, the generic compactification is not a simple Calabi-Yau manifold. So this geometric constraint rules out an interesting class of would-be models based on D3-branes in Calabi-Yau warped throats. But the general situation is richer, and there is no known geometric constraint sufficient to rule out gravitational waves from DBI inflation. However, as in any form of inflation the possibility of gravitational waves seems to require functional fine-tuning of the effective action.

Another challenge in obtaining DBI inflation from D-branes in a string compactification is the requirement that the effects producing the potential  $V(\phi)$  not backreact on the geometry probed by the brane, encoded in  $f(\phi)$ . This affects both large-field and small-field models. More precisely, the requirement is that once all the leading effects are included, the entire action (3.6) is known to the required accuracy in a solution with small generalized slow roll parameters (3.9). This is nontrivial to arrange, for the following reason.<sup>16</sup>

Start with the field theory coupled to gravity and to a hidden sector which breaks SUSY. Given the SUSY breaking, one generically generates a term  $m^2\phi^2$ . For example, in gravity mediation,  $m \sim F/M_{pl}$  where  $F$  is the SUSY-breaking F-term in the hidden sector. Now, generically the same effect would lift also the lightest modes in the throat, so the KK masses  $m_{KK} \sim (1/R)(r/R)$  must satisfy  $m_{KK} > m$ , where  $r$  is the radial coordinate. So the smallest value of  $r$ , let's call it  $r_{IR}$ , is  $r_{IR} = mR^2$ , which means the smallest value of the canonical field  $\phi$  is given by

$$\phi_{IR}^2 = \frac{N}{2\pi^2} m^2 \quad (4.25)$$

This closes off the IR end of the throat at the scale  $\phi_{IR}$ .

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<sup>16</sup>This argument is a four-dimensional effective field theory description of a comment of J. Maldacena.

Now, combine this with the requirement for inflation that the potential energy dominate over the kinetic energy:

$$V(\phi) > f^{-1}\gamma = \frac{2\pi^2}{N}\phi^4\gamma \quad (4.26)$$

For  $V(\phi) = m^2\phi^2$ , this implies  $\phi^2 < \frac{N}{2\pi^2\gamma}m^2$ . But this is lower than the IR cutoff  $\phi_{IR}$  just estimated in (4.25). One approach to evade this might be to consider not a universal gravity-mediated contribution generating  $V(\phi)$ , but something analogous to gauge mediation which couples preferentially to a brane probe. This might require a more elaborate setup for which the charge carried by the brane is different from the flux supporting the background AdS-like geometry.

Finally, in the case of a throat supported entirely by D3-brane charge  $N$ , the effective action for DBI inflation, when matched to data, requires an enormous value for this quantum number [67]. However, the relations between flux/brane quantum numbers and the parameters in the effective theory are very model-dependent. It is possible to obtain a much smaller set of input flux quantum numbers to obtain the same low energy effective DBI action governing wrapped branes probing other compactification geometries [92]. Work continues to combine such a choice of branes and geometry with a solution to the other problem of backreaction, and with an appropriate field range; recent concrete steps in this direction appeared in [92] discussed above, [130] (which includes angular motion) and [131] (which includes effects of multiple branes in DBI inflation). Once this is accomplished, analyses such as [132] could tie the observable parameters to some data of the compactification.

In general, in DBI as well as in slow roll inflation, there is a (roughly) one percent fine-tuning expected in order to ensure that the generalized slow roll parameters (3.9) are sufficiently small. The DBI action arises in a wide variety of circumstances in string theory, and it is an interesting open problem to exhibit one in which (3.6) arises explicitly.

More generally still, DBI inflation is likely to be one of a family of models with the shared feature that the kinetic terms are corrected by a series in  $\dot{\phi}^2/(\phi^n M_*^{4-n})$ , for some  $n > 1$ , generated by integrating out modes that become light as  $\phi \rightarrow 0$  (here  $M_*$  is a hard UV mass scale such as the KK, string or Planck mass). It is in some sense a fortunate accident that in the case of a brane probe we know how to sum up these effects to obtain the DBI action, but more generally *some* function  $P(X, \phi)$  (3.4) pertains in any situation of this kind. If all terms are of the same order in the resulting solutions, again the dynamics would tie the field velocity  $\dot{\phi}$  to the field  $\phi$  itself, leading to a similar mechanism for slowing the scalar field.

It would be extremely interesting to understand what a generic model of inflation looks like, in terms of  $P(X, \phi)$ . A primary difficulty is defining an appropriate, and universally acceptable, notion of genericity.<sup>17</sup> Moreover, it is plausibly the case that, even equipped with such a definition, the generic models in effective theories derived from string theory are not

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<sup>17</sup>It is certainly *not* suitable for this purpose to determine what is generic among proposed inflationary

entirely generic in quantum field theory. As we have explained, this is one of the routes by which string inflation, taken as an entire framework, could eventually be predictive.

The DBI form of the action for D-branes also leads to qualitatively interesting effects on tunneling [133] and, as argued very recently, on the cosmic string spectrum [134].

### 4.3 Inflation in M-theory

An interesting proposal closely analogous to D-brane inflation is M5-brane inflation, in which an M5-brane wrapping a curve in a Calabi-Yau space moves along the interval of a Hořava-Witten compactification. In the scenario of [135], a single M5-brane very close to one of the walls moves into it. The alternative idea of ‘assisted M5-brane inflation’ [136] is that a collection of many M5-branes, distributed along the interval of the compactification, can provide a more promising inflationary potential than that of a single M5-brane. Inflation occurs as the M5-branes disperse and move toward the boundary walls. In both cases, it would be important to understand whether there is a mechanism for avoiding the eta problem: the structure of the Kähler potential for the M5-brane position suggests that this difficulty will generically be present, as it is in D-brane inflation scenarios. A noteworthy feature of assisted M5-brane inflation is that, for a sufficiently large number of M5-branes and a suitably long interval, the tensor signal could be comparatively large [137]. It would be interesting to know whether these conditions can be satisfied in a consistent compactification in which the eta problem can be addressed at the same time.

### 4.4 Moduli inflation

#### 4.4.1 Inflation with Kähler moduli

Among the better-studied examples of moduli inflation are those that involve motion of the Kähler moduli in a flux compactification of type IIB string theory on a Calabi-Yau threefold. The Kähler moduli receive no potential from imaginary-self-dual fluxes [9], and the idea is that the potential induced by nonperturbative effects can be exponentially flat.

In Kähler moduli inflation [138], the inflaton is the size of a ‘blowup’ four-cycle in one of the large-volume compactifications of [139]. A variety of contributions to the potential are suppressed by the exponentially large overall volume of the compactification, so the leading-order potential turns out to be very simple and extremely flat. By the leading-order potential, we mean the potential derived by incorporating the effect of fluxes and nonperturbative effects in the superpotential, and including the known  $\alpha'$  corrections to the

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models, since humans are traditionally poor random number generators.

Kähler potential,

$$\mathcal{K} = -2M_{pl}^2 \log(\mathcal{V}(\phi) + \xi) \quad (4.27)$$

Here  $\mathcal{V}$  denotes the volume of the Calabi-Yau, which is a function of the inflaton  $\phi$ , because by assumption  $\phi$  is one of the Kähler moduli; the constant  $\xi$  is proportional to the Euler number of the Calabi-Yau.

An important unresolved question in this scenario is whether there exist further corrections to the Kähler potential, for example involving terms polynomial in the inflaton,

$$\mathcal{K} = -2M_{pl}^2 \log(\mathcal{V}(\phi) + \xi) + f(\phi)\mathcal{V}^{-c} \quad (4.28)$$

For suitable functions  $f$  and constants  $c$ , this correction curves the inflaton potential and leads to an eta problem. As noted in [138] and further explained in [140], such corrections are readily conceivable, and one might hope to compute them, perhaps along the lines of [89, 141, 142].

Kähler inflation as presently constructed is a small-field model, and as such is somewhat sensitive to the initial conditions. However, as argued in [140], a considerable fraction of randomly-chosen trajectories can give rise to substantial inflation.

In the type IIA orientifold constructions of [143, 103, 144], the complex structure moduli and Kähler moduli are on equal footing. A recent search for inflation in this context was unsuccessful [145], however there are further ingredients that can contribute to the potential energy.

#### 4.4.2 Inflation with axions

Because axions enjoy a shift symmetry that is unbroken to all orders in perturbation theory, they are natural candidates for inflaton fields [146]. The simplest scenario would be one in which a single axion has a large periodicity,  $f \gg M_{pl}$  [146]. At present this has yet to be achieved in string theory, and there are suggestive but incomplete arguments that this is impossible in general [147]. As a result, attempts to use string axions for inflation fall into two classes: those that use a small number of axions, and those that use many axions at once.

One proposal [148] is that under special circumstances, the effective decay constant of a linear combination of two axions will be super-Planckian, allowing a plausible realization of natural inflation in string theory.

Another scenario involving a small number of axions is (Better) Racetrack inflation [149, 150], in which a linear combination of the axions associated to two Kähler moduli rolls off of a saddle point of the potential. The background compactification is the KKLT-type construction of [151] in an orientifold of the Calabi-Yau threefold  $\mathbb{P}_{1,1,1,6,9}$ . Because the

moduli stabilization is comparatively well-understood, this is a rather explicit construction. One difficulty, however, is that the parameters chosen to achieve inflation in [150] are somewhat strained, as noted originally in [150]: in particular, the rank of one of the gauge groups whose strong gauge dynamics contributes to the nonperturbative superpotential was taken to be 258, which would have to correspond to a stack of 258 D7-branes. It is not obvious that this can be achieved in the construction of [151], and it would be worthwhile to find concrete compactifications, including the data of D7-brane stacks, that fulfill the promise of [150] (see also [152]).

Another approach [93] is to consider the simultaneous displacement of  $N \gg 1$  axions from their minima, and identify an effective inflaton with the Pythagorean sum of the individual displacements. For sufficiently large  $N$ , the resulting effective inflaton has a super-Planckian range. If the constituent axions all had exactly the same mass and same initial displacement, this model would be indistinguishable from Linde’s original chaotic inflation model. However, these conditions will certainly not be obeyed exactly; one therefore needs to know the axion mass spectrum in any given construction, and the observational predictions for a model with this spectrum. In [153] these problems were solved using random matrix theory, and it was shown that under very plausible assumptions, the spectrum of axion masses-squared in any KKLT compactification is described by the Marčenko-Pastur law. The single parameter characterizing the shape of this distribution turns out to be a ratio of Hodge numbers; the complicated and virtually uncomputable data associated with the details of the compactification becomes irrelevant in the large  $N$  limit [153]. The implication is that, although N-flation will not precisely coincide with single-field chaotic inflation, it will generically be only slightly – but measurably – different: in particular, the scalar spectrum is slightly more red in N-flation than in single-field  $m^2\phi^2$  inflation. For further investigations of the phenomenology of this scenario, see [154, 155, 156, 157, 158].

There are at least two important concerns about N-flation. The first is that the necessary compactifications are near the boundary of validity of the  $g_s$  and  $\alpha'$  expansions, and pack a tremendous ‘amount of topology’ into a small volume. In the four-dimensional theory, this manifests as a renormalization of the Newton constant, which may be thought of as being enhanced by the large number of species of particles circulating in loops. More precisely, one can determine the leading term in this renormalization from an  $\alpha'^3$  correction in ten dimensions. The problem is that higher corrections in the  $\alpha'$  and  $g_s$  expansions are not known at present, and could potentially spoil the success of the scenario.

The second concern [159] is that the real-part Kähler moduli, which control the volumes of four-cycles, will not find and remain in their minima as their axion partners roll towards the origin. This could give rise to important corrections to the potential, and in particular could negate the advantage resulting from the axions’ shift symmetry.

The constraints from reheating in N-flation were considered in [160]. A general problem

of closed string inflation that is particularly acute in N-flation is that in the presence of a large number of hidden sectors, it is typically difficult to ensure that the energy of the inflaton ends up primarily in the visible sector. In certain D-brane inflation models this problem is alleviated, because *both* the inflaton and the visible sector are well-localized in the compact space, and if they coincide at the end of inflation, strong reheating of the visible sector is then nearly automatic.

#### 4.4.3 *Inflation with complex structure moduli*

At present there are very few explicit scenarios involving motion of complex structure moduli. One reason is that, in the type IIB flux compactifications of [9], the complex structure moduli receive mass from the flux background, whereas the Kähler moduli and their axions do not; hence, the latter sector is arguably a more promising place to look for a relatively flat potential. However, it would be most interesting to understand the prospects for inflation with complex structure moduli, presumably in another class of compactifications.

### 4.5 Landscape inflation

Recent progress in understanding the potential on the configuration space of string compactifications, i.e. the ‘string landscape’, has led to a variety of original ideas for inflation. These proposals typically do not involve direct specification of an inflaton candidate in a concrete setup, but rather appeal to the general properties of the landscape, such as its high dimensionality and the large number of saddle points.

In New Old inflation [161, 162] (also known as Locked inflation), a scalar field oscillates repeatedly past a saddle point, and does not roll to the true vacuum – ending inflation – until the period of its oscillations becomes small compared to the timescale set by the tachyonic mass of the saddle. Given a large initial amplitude and a small tachyonic mass, this leads to prolonged inflation. However, the parameter space is strongly constrained by limits on formation of primordial black holes [163], and it has been argued that a long period of locked inflation must end through parametric resonance [164].

It has also been suggested [165] that two or more stages of inflation, at widely-separated scales, might involve less fine-tuning than a single period of inflation, and that such a history is plausible in the complicated potentials found in string theory.

Another scenario inspired by the idea of a complicated landscape of vacua is Chain inflation [166, 167, 168, 169].



## 4.6 Other ideas

String theory, and associated patterns of thought, have led to a diverse array of cosmological scenarios, some quite different from the inflationary models we have discussed here. Limitations of space, and of expertise, prevent us from covering the cyclic and ekpyrotic scenarios, mirage cosmology, cosmology of string and brane gases, and the Pre-big bang scenario, to name a few of the proposals most closely linked to string theory. For treatment of these subjects we refer the reader to [170, 171, 172, 173, 174, 175] and the references therein.

## 5 Dynamics of Moduli

Let us mention a few other roles that scalar fields in field theory and string theory can play in cosmology. First, the dynamics of moduli is relevant for the problem of vacuum selection and the question of initial conditions for inflation. More generally, rolling scalar fields can drive non-inflationary cosmological phases, and by characterizing the possibilities in this class, one can understand the scope of cosmological behaviors that are allowed by string theory, as a UV completion of gravity.

### 5.1 Effects of light species at weak and strong coupling

In a Lagrangian with multiple scalar fields, scalar-scalar interactions are widespread. For example, two scalars  $\phi, \chi$  often interact via the quartic coupling

$$\Delta\mathcal{L} = g^2\phi^2\chi^2 \tag{5.29}$$

Consider a background in which  $\phi$  is rolling through its configuration space. The interaction (5.29) leads to a  $\phi$ -dependent mass for  $\chi$ . That is, the Hamiltonian for  $\chi$  is time-dependent in a background solution in which  $\phi$  is rolling. This leads to a backreaction on the solution for  $\phi$  itself. A similar effect holds for  $\chi$  particles of other spins; a canonical situation with vector  $\chi$ 's arises when  $\phi$  is a Higgs field for the corresponding gauge symmetry.

There are two basic ways in which this happens: (i) virtual  $\chi$  quanta circulating in loops renormalize the effective action for  $\phi$  (as discussed in regard to DBI inflation in §2 and §4.2.2) and (ii) the time-dependent masses and couplings lead to the production of on-shell  $\chi$  quanta [176, 177, 178, 179, 180]. In the latter case, the energy density of the resulting gas of  $\chi$  particles is minimized at the point  $\phi = 0$  where they are massless, which leads to a force on  $\phi$  drawing it toward this point.

At strong 't Hooft coupling in AdS/CFT systems, (i) is a controlled process and dominates over (ii). At weak coupling, (ii) is a controlled process that dominates over (i). In both limits (and probably also in the intermediate regime where both occur), the effect is to trap  $\phi$  near

points with extra light species  $\chi$ . (See [181] for other work on enhanced symmetry points and the moduli problem.)

This trapping effect in case (ii) only pertains when the kinetic energy transferred into  $\chi$  particles dominates over the potential energy. Hence, it may play a role in any epoch in which scalar fields roll relatively freely. In an expanding universe, the gas of  $\chi$  particles is diluted over time, weakening the trapping effect, as discussed in detail in [178].

The above effect occurs at the level of field theory, but also extends to situations in which the  $\chi$  fields are extended strings, in such a way that oscillator modes enhance the effect when weakly-coupled branes collide relativistically [182]. Early in the study of string cosmology it was realized that the presence of a gas of extended objects (strings and branes) could affect the evolution in interesting ways [183] in the presence of nontrivial topology. For example, in the heterotic theory on a torus, winding strings  $\chi$  become light and enhance the gauge symmetry at the self-dual radius. A somewhat similar effect is relevant for closed string winding modes near spacelike singularities, as discussed in §2.

In their regime of applicability, these kinetic effects provide a dynamical mechanism favoring points with light species. It is important to note, however, that this does *not* in itself stabilize the moduli; the potential energy dominates at late times.

Another interesting phase of string cosmology is that which results from the annihilation of unstable D-branes. This is a process that is affected strongly by  $\alpha'$  effects which have been extensively studied, and hence provides a setting incorporating inherently string-theoretic behavior into cosmology. For a review of this direction, see [184].

## 5.2 Other cosmological phases

String theory has a rich set of weakly coupled limits, unified by various dualities and by topology-changing and even dimension-changing transitions (such as the recent classes of examples [39, 41, 40, 185] discussed in §2.2). As also discussed above, in every known model of inflation, a certain amount of fine-tuning is required from the low energy point of view, and the effective action derived from string theory does not appear to yield miraculous top-down cancellations of the generalized slow roll parameters. In particular, in weak-coupling asymptotic regimes of scalar field space (such as large volume  $\mathcal{V} \gg l_s^{D-4}$  and weak string coupling  $g_s \ll 1$ ), the kinetic terms are canonical and the potential slopes toward zero too quickly for inflation.

The perturbative potential is exponential in the canonically-normalized scalar fields (linear combinations of the dilaton  $\Phi = M_{pl} \log(g_s)$ , the radion  $\sigma \equiv M_{pl} \log(\mathcal{V})$ , and so on). The form of this potential leads to two interesting effects. First, the generic weakly-coupled rolling scalar solution is not inflation, but rather a rather simple quintessence model with  $w = -2/3$  (on the boundary between acceleration and deceleration). The leading term

in the moduli potential scales like  $g_s^2(D - 10)/\mathcal{V}$ . For  $D > 10$  with a Ricci-flat internal compactification there is an  $\alpha'$ -exact tree-level solution [186, 187] with scale factor  $a(t) \propto t$  linear in FRW proper time  $t$  (and with the dilaton linear in conformal (string frame) time  $X^0\sqrt{D} \sim l_s \log(t/l_s)$ ). In this  $a(t) \propto t$  phase arising generically in weakly-coupled string theory, modes neither enter nor leave the horizon, and the question of the spectrum of density perturbations reverts to one of initial conditions, tying it to the physics closer to the initial singularity (for recent studies of this, see [41, 185, 40]). The second intriguing feature of these weakly-coupled backgrounds is the following. A canonically-normalized field with a negative exponential potential has a scale-invariant power spectrum in Minkowski space, and also in any background in which its energy density is subdominant in driving the expansion of the universe. (See [188] and references therein for a recent discussion of this.) Backgrounds with a compactification manifold of positive scalar curvature, or with subcritical dimensionality, yield a negative exponential potential coming from string theory.

Work continues aimed at understanding the role of these more general backgrounds. Because of the genericity of the exponential potential terms<sup>18</sup> and the possibility of generating scale-invariant perturbations from them, it would be very interesting to understand if the generic effective theory descending from string theory yields an alternative to inflation. However, this is extremely challenging – at present inflation fits the observations in numerous interconnected ways, making it very difficult to envision a competitive alternative.

## 6 Dark Energy in String Theory

The discovery that the expansion of the universe is accelerating is among the most significant of recent times. It makes untenable the old hope that some mechanism might set the cosmological constant precisely to zero, and it demands an explanation of why the scale of dark energy is nonzero, yet so small compared to the Planck scale, or indeed even to the GeV scale.

Our present understanding of string theory, albeit incomplete, meshes with a nonzero value for the cosmological constant. There is a “discretuum” of contributions to the moduli potential arising from choices of discrete quantum numbers (dimensionality, topology, fluxes, brane and orientifold numbers, and so on) [20] which plausibly yields enough freedom to tune the cosmological constant finely, but not precisely to zero. This argument has two caveats: (1) it assumes moduli stabilization, and (2) it assumes that there are no conspiracies affecting this tuning process in the realistic window in which  $\geq$  TeV scale quantum corrections would need to be tuned almost away. Point (1) has been addressed extensively in recent and

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<sup>18</sup>In [189] it is proposed that suitable collections of exponential potentials produce inflationary models which, although still fine-tuned, are arguably numerous.

ongoing work, while point (2) remains inaccessible to explicit analysis.

Various mechanisms of moduli stabilization have been the subject of several useful lectures and reviews, such as [14, 15, 16, 17, 18], so we will only give a qualitative picture here. The basic problem is that the potential slopes to zero in weakly coupled limits such as large radius (in geometric models) and weak string coupling (in corners of M-theory with a perturbative string description).

If we focus on geometrical compactifications near weak-coupling limits, it is straightforward to see that sources of positive energy in four-dimensional effective theories derived from string compactifications source an expansion of the internal space. This can be understood as follows. Begin with a source of positive energy in  $D$  dimensions, including the tree-level cosmological term proportional to  $D - 10$ , as well as additional sources such as brane or flux configurations, and dimensionally reduce to four-dimensional Einstein frame. The volume  $\mathcal{V}$  of the internal space enters the rescaling to Einstein frame in such a way that these higher-dimensional energy sources, when reduced to four-dimensional potentials  $\mathcal{U}_i$ , scale inversely with the volume,

$$\mathcal{U}_i = \frac{c_i}{\mathcal{V}^{\alpha_i}} \quad (6.30)$$

with  $\alpha_i$  positive and  $c_i$  independent of  $\mathcal{V}$ . Hence, sources of positive energy in string theory tend to yield a runaway behavior, driving the volume to larger values. The result is that a stable or metastable de Sitter vacuum is possible only in the presence of a counterbalancing force that prevents decompactification. Similar statements apply to the string coupling. In other words, the simplest way to obtain de Sitter space requires three competing terms in the potential expanded about weak coupling:

$$\mathcal{U} \sim ag^2 - bg^3 + cg^4 \dots \quad (6.31)$$

where  $g$  represents the string coupling and the (moduli-dependent) coefficients  $a, b, c$  are all positive at a local minimum of the potential; a similar expansion obtains for inverse volumes and any other runaway moduli in the problem [190]. A little algebra reveals that for a de Sitter solution, one needs sufficient freedom to tune the coefficients at the minimum to obtain  $0 < (4ac/b^2) - 1 < 1/8$ . In particular, the negative term  $-bg^3$  needs to be sufficiently strong relative to the leading  $ag^2$  term, and involves ingredients (such as orientifold planes or closely-related objects in all known constructions) going beyond GR or supergravity. As emphasized in [10], this leads to solutions which are only *meta*-stable, a result that follows rather generally from considerations of thermal effects in local de Sitter solutions [12, 191]. For a recent analysis of decay rates in some constructions, see [192].

In general, it is essential to recognize that one must introduce a small or large number by hand in order to ensure that different orders in perturbation theory (as well as nonperturbative effects) can compete with each other to fix the runaway moduli. To ensure a small value of the vacuum energy at the minimum, much further tuning would be required.

In the last several years this problem has been the focus of intense efforts, and a range of mechanisms have been proposed at various scales of supersymmetry breaking [11, 12, 193].<sup>19</sup> In particular, the proposal of [9, 12] (and subsequent work) builds up from a Ricci-flat internal space – a special choice which is compatible with traditionally natural solutions to the hierarchy problem: low energy supersymmetry combined with Randall-Sundrum warped extra dimensions. The others [11, 193] build from the leading terms in the moduli potential (including the positive potential energy arising from supercriticality and/or negative curvature), arising from a much wider range of choices of topologies and dimensionalities for the internal space – but they do not incorporate a traditionally natural solution to the weak hierarchy problem.

One interesting tradeoff in the subject is that the higher scales of SUSY breaking permit more terms in the effective action. This simplifies the analysis in some ways and complicates it in others. It means on the one hand that more competing forces are available in perturbation theory in  $g$ , allowing for metastabilization at this level. On the other hand, more corrections are allowed and must be bounded in order to exhibit a well-defined approximation scheme. In the low-energy SUSY framework of [9, 12], SUSY constrains the effective action so that one needs to use a non-perturbative contribution, competing with a perturbative flux superpotential. On the other hand, SUSY helps stabilize against decays and corrections, simplifying that part of the analysis. In any case, at any scale of SUSY breaking, control is obtained via perturbation theory, by ensuring that  $\alpha'$  and  $g$  perturbations about the background solution are small.

As with the models of inflation discussed previously, we wish to make clear some of the open issues in this area. A concern about the framework [11], as mentioned in [11], is the large number of RR-sector species at high dimension  $D$ , though as in the critical dimension one expects Chern-Simons couplings to lift many RR axions,<sup>20</sup> and loop effects in high-dimensional field theory are suppressed by factors of  $1/D!$  at large  $D$  [194]. An open question about the framework [9, 12] and also [193] is the role of the full complement of  $\mathcal{R}^4$  terms. A specific quartic curvature term related to the Euler character of an F-theory fourfold is used in the construction. This term has a topological reason to have a large coefficient, so it is reasonable to focus first on its effects. As reviewed in detail in [17], a subset of the remaining quartic curvature terms has been computed in a number of important works, and the result agrees with the expectation that the Euler character term dominates. Even so, it would be interesting to understand explicitly whether other  $\mathcal{R}^4$  terms might compete in some circumstances, and if so how they affect the solution.

The discussion of the landscape also led to some spurious objections to the model-building efforts reviewed here. Some physicists objected to the use of RR fields. RR fields appear

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<sup>19</sup>These works followed early works on flux compactification, such as [6, 7, 8, 9, 10].

<sup>20</sup>E.S. thanks S. Hellerman for this comment.

in the simplest flux compactifications – Freund-Rubin models – which admit an exact formulation based on AdS/CFT, and their use fits into standard effective field theory. Similar comments apply to the objection to models based on gaugino condensation and other non-perturbative effects; the effects included in [12] are standard contributions in the low energy effective theory which forms the basis of a well-defined approximation scheme in the models. Some physicists objected to the supercritical examples based on the claim that these are not part of M theory. This is incorrect. For recent analyses exhibiting the dynamical connection between critical and non-critical corners of string theory see [39, 41] (reviewed above in §2).<sup>21</sup> In particular, the ten-dimensional superstring on an expanding compact negatively curved space has a supercritical effective central charge; Hubble expansion suffices to exhibit the transition from supercritical to critical regimes of string theory. Moreover, tachyons tuned to turn on along a lightlike direction provide an  $\alpha'$ -exact method for exhibiting dynamical connections between highly supercritical and critical limits of string theory. Nonetheless, although some of the objections have been incorrect, it is fair to say that all models in the landscape are somewhat complicated, and it is important to bear in mind the possibility – however unlikely – that some new top-down consistency criterion will eliminate some or all of the proposed solutions.

It will be very interesting to learn from the LHC whether low-energy supersymmetry governs the electroweak scale; the landscape of string vacua has reinvigorated discussion of the open question of how similar (or not) are the problems of explaining the electroweak and cosmological constant scales (see for example [195]). In any case, although it is now clear that the requisite competing forces are available in reasonably well-understood compactifications, nothing close to a complete picture of the string landscape presently exists. It would be interesting to develop completely explicit examples of  $dS_4$  in string theory, as has been achieved for  $AdS_4$  flux compactifications in [151, 196, 197] and especially simply in [143]; work continues in this direction (e.g. [198]). However, explicit, controlled weakly coupled models of de Sitter along these lines would not be realistic, since that would require explicit fine-tuned cancellation of loops of Standard Model particles. For this and other reasons, another important direction, which we will not review here, is the quest for concrete holographic duals of landscape models.

Of course it would be spectacular to find a first-principles prediction of the scale of dark energy rather than accommodating it as a selection effect [5], but this is extremely challenging [199]. At the time of this writing, no compelling proposal exists, despite some interesting attempts.<sup>22</sup> Moreover, the success of inflationary cosmology as well as the presence of a

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<sup>21</sup>It has been known since the early years of string theory that tachyon condensation lowers the effective central charge, the only invariant consistency condition being that the total central charge (matter plus ghost) vanishes on the worldsheet.

<sup>22</sup>One related point to emphasize is that it appears much simpler to obtain a local metastable minimum for

discretuum of string vacua appears to point instead toward a global cosmology containing a wide variety of regions with different local cosmological parameters.<sup>23</sup>

## 7 Conclusions

The outlook for string cosmology is rather bright: at least for the near future, experimental and theoretical progress are likely to be rapid. The coming generation of cosmological experiments will probably rule out the great majority of string inflation scenarios, as well as most of their alternatives, allowing a more efficient focus on the surviving models. Steady progress in string theory should ensure that cosmological model-building ten years from now will be substantially more realistic and rigorous than it is now. We also anticipate progress towards a more comprehensive theory of initial conditions and spacelike singularities.

One of the lessons of the subject so far, it seems to us, is the presence of serendipitous connections between formal developments and observational opportunities. Focusing on mechanisms (such as moduli stabilization effects and warping, or the speed limit on brane probes) led to inflation scenarios with detailed observational predictions (such as viable cosmic string tensions, or non-Gaussian corrections to the CMB) in a way that would have been difficult to predict from the start. Moreover, spinoffs of string theory such as novel inflation mechanisms may be considered independently within effective field theory whether or not they are realized concretely or generically in string theory—supersymmetry being a famous example of this within particle physics. Of course these connections are only truly exciting if observed in experiments, but they also sometimes yield important conceptual lessons in the meantime.

Despite these promising signs, it remains to be seen whether this endeavor will lead to genuine contact between experiment and Planck-scale physics. In many scenarios, inflation is described by a well-controlled, albeit fine-tuned, effective field theory Lagrangian, and inflation lasts long enough to obscure all evidence of a pre-inflationary stage. If we live in such a universe, cosmological observations can, at best, teach us about the nature of the inflaton, but will provide few clues about more fundamental physics, except perhaps through the enduring mystery of dark energy.

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the moduli, rather than further fine-tuning to obtain quintessence fields or other very light scalars; however, interesting and testable scenarios such as [200] have been explored.

<sup>23</sup>There are ideas for seeking observational evidence for a tunneling transition preceding our local cosmology [201].

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